

A cannon ball is fired from the mouth of a cannon which is six feet off the ground. If the vertical velocity is 50ft/sec and the horizontal velocity is 70ft/sec how far does it fly before it hits the ground?

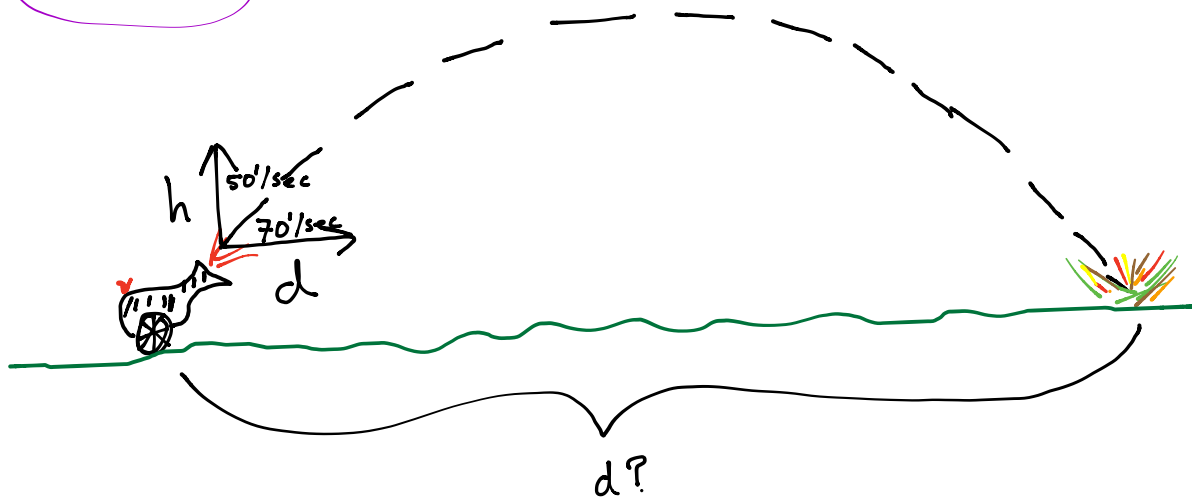
$$h = -\frac{1}{2}at^2 + v_0t + s_0 = -16t^2 + 50t + 6 = 0, \text{ then}$$

$$d = v_1t = 70t$$

$$\text{if } t = 3.24,$$

$$d = 70(3.24) \\ = 226.8$$

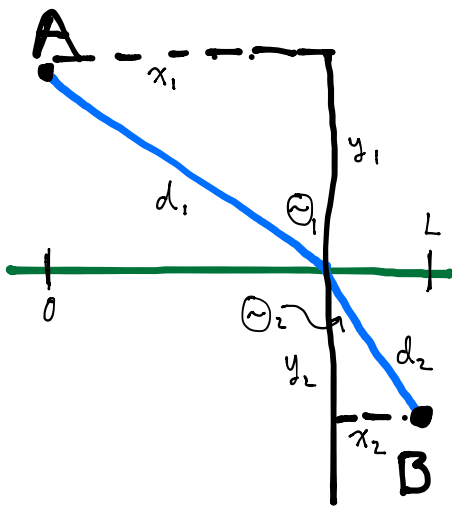
$$t = \frac{-50 \pm \sqrt{50^2 - 4(-16)(6)}}{-32} = 3.24$$



Snell's Law states that as light passes from one medium to another

$$\frac{\sin(\theta_1)}{c_1} = \frac{\sin(\theta_2)}{c_2}$$

where θ_1 and c_1 are the angle of incidence and speed of light in the first medium and θ_2 and c_2 are the angle of refraction and speed of light in the second. Prove that Snell's Law holds by minimizing the travel time of light from a point in the first medium to a point in the second.



$$T = \sqrt{x_1^2 + y_1^2} + \sqrt{x_2^2 + y_2^2}$$

$$\left. \begin{aligned} y_1 &= y_2 = 1 \\ x_2 &= L - x_1 \\ &\quad \downarrow \\ &\quad x \end{aligned} \right\}$$

$$\Rightarrow T = \sqrt{x^2 + 1} + \sqrt{(L-x)^2 + 1}$$

$$d = vt = t = d/v$$

$$t = \frac{d_1}{c_1} + \frac{d_2}{c_2} = \frac{\sqrt{x^2 + 1}}{c_1} + \frac{\sqrt{(L-x)^2 + 1}}{c_2} \Rightarrow \frac{dt}{dx} = \frac{1}{c_1} \cdot \frac{x}{\sqrt{x^2 + 1}} - \frac{1}{c_2} \cdot \frac{(L-x) \cdot (-1)}{\sqrt{(L-x)^2 + 1}}$$

$$\text{SOH CAHTOA} \rightarrow \sin(\theta_1) = \frac{x_1}{d_1}$$

$$\sin(\theta_2) = \frac{x_2}{d_2}$$

$$\Rightarrow \frac{dt}{dx} = \frac{1}{c_1} \cdot \sin(\theta_1) - \frac{1}{c_2} \sin(\theta_2) = 0$$

$$\Rightarrow \frac{\sin(\theta_1)}{c_1} = \frac{\sin(\theta_2)}{c_2} \quad \checkmark$$